MATH 205 Homework Supplement

In the following problems, $I_k \subset \mathbb{R}^k$ is the k-cell $[0,1]^k$, and Q_k is the k-simplex. You should use the notation (u_1, \ldots, u_k) to denote a point in I_k or Q_k .

In each of the following problems, ω is a k-form and Φ is a k-surface. You should write

 $\int_{\Phi} \omega$

in terms of 1-dimensional integrals involving the variables u_i only. In particular, you should compute all the relevant partial derivatives and evaluate the relevant determinants. There is no need to evaluate the one-dimensional integrals.

- **1.** $\omega = x_2^2 dx_1 + x_1 dx_2, \ \Phi(u) = (\cos u, \sin u), \ 0 \le u \le 1.$
- **2.** $\omega = x_1 x_2 dx_1 \wedge dx_2 + \sin x_3 dx_1 \wedge dx_3, \Phi : Q_2 \to \mathbb{R}^3, \Phi(u_1, u_2) = (u_1 + u_2, e^{u_2}, 0).$
- **3.** $\omega = dx_1 \wedge dx_2 \wedge dx_3, \ \Phi : Q_3 \to \mathbb{R}^3, \ \Phi(u_1, u_2, u_3) = (u_1 u_2, u_2, u_3^2).$