

**Abstract:** We prove that if  $X$  is a loop space and the integral homology of  $X$  is finitely generated as an abelian group, then  $X$  is homotopy equivalent to a closed, smooth, parallelisable manifold. This is joint work with Tilman Bauer, Nitu Kitchloo and Dietrich Notbohm.